$$S = \mathrm{diag}(-1, 1)$$

